

**JAWAHARLAL NEHRU TECHNOLOGICAL UNIVERSITY HYDERABAD**  
**II.B.TECH - I SEMESTER REGULAR EXAMINATIONS NOVEMBER, 2009**  
**MATHEMATICAL FOUNDATIONS OF COMPUTER SCIENCE**  
**(Common to CSE, IT, CSS)**

Time: 3hours

Max.Marks:80

**Answer any FIVE questions**  
**All questions carry equal marks**

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1. Explain following terms:
  - i) Tautology
  - ii) Contra positive
  - iii) Universal valid formula
  - iv) Contradiction

[4\*4=16]
2. a) What is predicate calculus? What is its significance? Give example for 3-place, 4-place & 5-place predicates.  
 b) Prove validity of following argument using propositional logic:  

$$A \rightarrow (B \rightarrow C), B \rightarrow (C \rightarrow D) \Rightarrow A \rightarrow (B \rightarrow D)$$

[8+8]
3. a) Let the relation  $R = \{ (1,2), (2,3), (2,4) \}$  on the set  $\{ 1,2,3,4 \}$ . Obtain transitive closure of R.  
 b) What is the domain of the function :  $f(x) = \cos \log \left\{ \frac{\sqrt{2-x^2}}{(1-x)} \right\}$ 

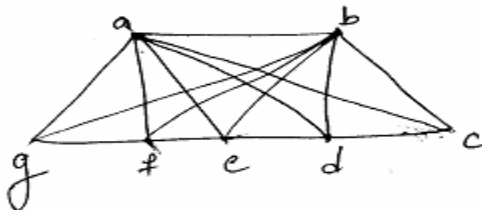
[8+8]
4. a) Show that for any commutative monoid  $(m, *)$ , the set of idempotent elements of m forms a submonoid.  
 b) Explain Epimorphism & Monomorphism in detail.
 

[8+8]
5. a) How many ways are there to roll two distinguishable dice to yield a sum that is divisible by 2?  
 b) State & prove Binomial theorem.
 

[8+8]
6. a) Compute a simple expression for the power series:  

$$\sum_{n=1}^{\infty} (n+1)(n+1)(n) X^n$$
 b) Solve  $a_n - 6a_{n-1} + 8a_{n-2} = n4^n$  where  $a_0 = 8, a_1 = 22$ 

[8+8]
7. a) What is planar graph? Show that following graph is planar.



- b) Draw following graphs : i)  $C_5$  ii)  $K_6$  iii)  $K_{3,3}$  iv)  $W_6$ 

[8+8]
8. a) Derive an algorithm for constructing Euler circuit in directed & non-directed graph  
 b) Distinguish between following terms
  - i) Cycle and Circuits.
  - ii) Hamiltonian graph & Euler graph.

[8+8]